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DAMAGE CHARACTERISTICS OF AN  
INFINITE CYLINDRICAL SHELL  
EXCITED BY A TRANSIENT ACOUSTIC WAVE.

by

T. L. Geers  
C.-L. Yen

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# ABSTRACT

An analytical/computational technique previously developed for determining the geometrically and constitutively nonlinear response of a submerged, infinite cylindrical shell to a transverse, transient acoustic wave is used to study the damage behavior of the shell. Incident waves of rectangular pressure-profile are considered, nonlinear transient response computations are performed, and damage results are described in terms of iso-damage curves based on extensional set strain. Results generated through the use of the doubly asymptotic approximation for treatment of the fluid-structure interaction differ appreciably from their exact counterparts.

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## Section 1 INTRODUCTION

An analytical/computational technique has recently been developed for determining the geometrically and constitutively nonlinear response of an infinite cylindrical shell to a transverse, transient acoustic wave [1]. The technique involves the use of the structural analyzer DYNAPLAS [2] to treat shell response, and the use of the residual potential formulation [3] to treat the fluid-structure interaction; it has been implemented in the form of a coupled software assembly named RPF-DYNA.

In this study, RPF-DYNA has been used to investigate the damage behavior of a particular shell for incident plane waves of rectangular pressure-profile. The shell exhibits elastic/perfectly plastic material behavior and is characterized by hydrostatic elastic-critical-buckling and elastic-limit pressures that are virtually equal. Because the deformational response of the shell is dominated by extensional motion, damage results are described in terms of iso-damage curves [4] based on extensional set strain.

Iso-damage curves are also constructed for the shell that pertain to the use of the doubly asymptotic approximation (DAA) [5,6] for treatment of the fluid-structure interaction. This approximation, which is the basis for fluid-structure interaction analysis in a number of existing codes [7-12], is asymptotically exact for both low- and high-frequency fluid motions, effecting a smooth transition in the intermediate frequency range. Its computational advantage is that it may be expressed as a matrix ordinary differential equation without requiring discretization of the infinite volume of fluid surrounding the structure.

## Section 2 RESPONSE CALCULATIONS

Consider the two-dimensional, plane-strain motions of the submerged, infinite, circular cylindrical shell of Figure 1. The shell is excited by a transient acoustic wave that first contacts the shell at  $\theta = \pi$ . During the resulting fluid-structure interaction, shell behavior may involve both geometric and constitutive nonlinearity.

### 2.1 NONDIMENSIONAL RESPONSE EQUATIONS

Following an expansion of the pertinent response variables in circumferential Fourier series, nondimensional response equations for each Fourier harmonic may be derived as [1]

$$\begin{aligned} \left(\frac{\rho_0}{\rho}\right)\left(\frac{h}{a}\right)\ddot{w}_0 + \dot{w}_0 + f_0(v, w) &= \dot{\phi}_{I0} + u_{I0} - \frac{1}{2}\dot{\phi}_{S0} + \phi_{R0} \\ \left(\frac{\rho_0}{\rho}\right)\left(\frac{h}{a}\right)\ddot{w}_n + \dot{w}_n + f_{wn}(v, w) &= \dot{\phi}_{In} + u_{In} - \frac{1}{2}\dot{\phi}_{Sn} + \phi_{Rn} \\ &\quad + (\dot{\phi}_{I0} + \dot{\phi}_{S0})(nv_n + w_n) + \ddot{w}_0 w_n, \quad n \geq 1 \end{aligned} \quad (1)$$

$$\left(\frac{\rho_0}{\rho}\right)\left(\frac{h}{a}\right)\ddot{v}_n + f_{vn}(v, w) = (\dot{\phi}_{I0} + \dot{\phi}_{S0})(v_n + nw_n), \quad n \geq 1$$

$$\dot{\phi}_{Sn} + \frac{1}{2}\dot{\phi}_{Sn} = u_{In} - \dot{w}_n + \phi_{Rn}$$

$$\phi_{Rn} = -r_n * \phi_{Sn}$$

where  $v_n$  and  $w_n$  are circumferential and radial shell-displacement harmonics, respectively,  $f_0$ ,  $f_{vn}$  and  $f_{wn}$  are stiffness-force harmonics computed within DYNAPLAS that involve linear-elastic, geometrically nonlinear and constitutively nonlinear behavior,  $\phi_{In}$  and  $u_{In}$  are fluid-velocity-potential and radial-fluid-particle-

velocity harmonics for the incident-wave field at the shell's wet surface, respectively,  $\phi_{Sn}$  and  $\phi_{Rn}$  are wet-surface scattered-wave-velocity-potential and residual-velocity-potential harmonics, respectively,  $r_n$  is a known time-dependent characteristic function [3], and where  $n$  is the Fourier index, a dot denotes temporal differentiation and the asterisk denotes temporal convolution. All of the quantities and operations in (1) are nondimensional, normalized in accordance with the convention

$$w_{n.d.} = w/a, t_{n.d.} = ct/a, \phi_{n.d.} = \phi/ac, f_{n.d.} = f/\rho c^2 \quad (2)$$

For  $n=0$ , (1) contains three equations for the three unknowns  $w_0$ ,  $\phi_{S0}$  and  $\phi_{R0}$ , while for each  $n \geq 1$ , (1) contains four equations for the four unknowns  $v_n$ ,  $w_n$ ,  $\phi_{Sn}$  and  $\phi_{Rn}$ . Here, as in [1], the first three of (1) are solved with the half-step central-difference algorithm, the fourth of (1) is solved with a fourth-order Runge-Kutta scheme, and the last of (1) is solved by trapezoidal integration. This procedure possesses satisfactory accuracy, stability and efficiency characteristics.

## 2.2 DAMAGE BEHAVIOR

The damage behavior of a particular cylindrical shell with elastic/perfectly plastic material behavior is studied by calculating numerous transient response histories for incident plane waves of rectangular pressure-profile. The shell chosen is the single-layer "compromise shell" of [1], whose inertial, elastic, hydrostatic-elastic-stability, and extensional elastic-limit characteristics match those of a steel sandwich shell, which exhibits in plane-strain fashion the enhanced flexural stiffness properties of stiffened shells. As discussed in [1], the use of the compromise shell is necessitated by the limitation of DYNAPLAS analysis capability to single-layer shells. Table 1 shows the basis of equivalence for the two shells; the only discrepancies pertain to inelastic flexural characteristics, which, as seen below, are of minor significance. Note that the yield-stress value  $\sigma_y$  is such that the shells' hydrostatic elastic-limit pressure  $P_0$  (whose non-dimensional value is identical to the elastic-limit membrane stress-resultant  $N_y$ ) exceeds their static-elastic-stability pressure  $P_0$  by 2.4%.

The response variable chosen for damage assessment is circumferential extensional (or membrane) set strain, for two reasons. First, as discussed in [1], the inelastic response of this shell is dominated by extensional motion. Second, extensional shell response almost always reaches its late-time asymptotic limit within five shell-envelopment periods following the passage of the incident wave over the shell; this is in contrast to flexural shell response, which exhibits low-frequency oscillatory behavior for extremely long times. Hence a systematic treatment of flexural set strain requires that each transient response calculation be followed by a dynamic-relaxation calculation involving the introduction of artificial damping to damp out the oscillations. In view of the first reason, the results thus obtained are probably not worth the effort.

Representative inner-fiber and outer-fiber strain response histories are shown in Figure 2. In this case, the magnitude of the incident rectangular wave is five times the static-elastic-stability pressure ( $P_I = 5 P_C$ ) and the duration of the wave is equal to the shell-envelopment period ( $T_I = 2$ ). For these input parameters, extensional set strain is largest in magnitude at  $\theta = 0$ . From Figure 2,  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}} = 4.8\%$ , while  $|\epsilon_{\text{flex}}^{\text{set}}|_{\text{max}} \approx 0.15\%$ ; hence peak flexural strain is only 3% of peak extensional strain in this case.

Highly unrepresentative inner-fiber and outer-fiber strain response histories are shown in Figure 3. In this case, for which  $P_I = 1.8 P_C$  and  $T_I = 10$ , extensional set strain is largest in magnitude at  $\theta = 70^\circ$ . From the figure,  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}} = 6.0\%$ , while  $|\epsilon_{\text{flex}}^{\text{set}}|_{\text{max}} \approx 2.5\%$ ; hence peak flexural strain is about 40% of peak extensional strain in this case.

A more comprehensive picture of the inelastic response results obtained in this study is provided in Table 2. This table summarizes the results obtained in 18 of the more than 50 RPF-DYNA transient response calculations performed. Six quantities are shown for each response calculation, as indicated in the format statement.

Table 2 shows that the set-strain field in the shell is dominated by the  $n = 0$  harmonic, with the  $n = 1$  and  $n = 2$  extensional harmonics making modest



contributions and the higher extensional harmonics contributing very little. Flexural set strain is significant only in a few cases. Maximum extensional set strain usually occurs on the side of the shell that faces away from the incoming wave.

### 2.3 ISO-DAMAGE CURVES

Calculated values of  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}}$  are shown as circled dots in Figure 4, plotted as functions of magnitude ( $P_I$ ) and duration ( $T_I$ ) of the incident rectangular wave. (Recall that  $P_c$  is the elastic-critical-buckling pressure for this shell, which is nearly equal to its hydrostatic elastic-limit pressure). The  $T_I = \text{const.}$  curves that connect the dots permit the accurate estimation of six combinations of  $P_I$  and  $T_I$  that yield a prescribed value of  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}}$ . The selection of five such values then leads to the iso-damage curves of Figure 5.

Figure 5 shows curves of constant  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}}$  plotted in terms of the pressure magnitude and total impulse that completely characterize an incident rectangular wave. Although the curves exhibit the general characteristics of iso-damage curves, i.e., transition from vertical asymptotes for short pulses to horizontal asymptotes for long pulses, they do not possess the simple hyperbolic shapes produced by simple mechanical systems [4].

In Figure 5, each iso-damage curve appears to consist of two damage branches, one for pulses with  $T_I \lesssim 3$  and another for pulses with  $T_I \gtrsim 3$ . The distinctly positive slopes characterizing the high-strain  $T_I \lesssim 3$  branches for  $T_I \gtrsim 1.5$  produce an unexpected characteristic, viz., that a decrease in pressure magnitude,  $P_I$ , for fixed impulse,  $P_I T_I$ , may produce an increase in peak extensional set strain,  $|\epsilon_{\text{ext}}^{\text{set}}|_{\text{max}}$ . This is undoubtedly associated with a resonance condition where the shell is especially susceptible to pulses with durations comparable to the shell-envelope period.

### 2.4 DOUBLY ASYMPTOTIC APPROXIMATION

As discussed earlier, the doubly asymptotic approximation (DAA) has been extensively used in problems of this type for treatment of the fluid-structure

interaction. Utilization of the DAA in the present problem merely involves taking  $\phi_{Rn} = 0$  and replacing the coefficients  $\frac{1}{2}$  in (1) by  $n$ . As mentioned in [1], the DAA reduces to the plane wave approximation (PWA) for  $n = 0$  in this case.

Extensive DAA-DYNA calculations have been performed for the compromise shell of Table 1. The results of these calculations exhibit dominance of the  $n = 0$  harmonic, as previously seen in the RPF-DYNA results; however,  $n = 1$  strain response emerges in the DAA-DYNA calculations as almost as significant as  $n = 0$  strain response. Contributions to total strain by the higher harmonics, whether extensional or flexural, are generally small in the DAA-DYNA calculations.

Values of  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$  obtained from the DAA-DYNA calculations are shown as circled dots in Figure 6, plotted in the manner of Figure 4. In contrast to their RPF-DYNA counterparts, these results indicate that peak extensional set strain usually occurs on the side of the shell that faces toward the incoming wave.

The same procedure that produced the iso-damage curves of Figure 5 from the  $T_I = \text{const.}$  curves of Figure 4 has been used to produce the iso-damage curves of Figure 7 from the  $T_I = \text{const.}$  curves of Figure 6. Even a cursory comparison of Figures 5 and 7 reveals marked differences between the RPF-DYNA and DAA-DYNA curves. First, and most important, the DAA-DYNA curves for higher-strain values lie well to the right of and above their RPF-DYNA counterparts, which means that use of the DAA may lead to serious underpredictions of damage levels. Second, and less important, the DAA-DYNA curves do not exhibit the resonance behavior observed in the RPF-DYNA curves.

Figs. 5 and 7 demonstrate the general inadequacy of the DAA for treatment of the fluid-structure interaction in the present problem. As mentioned in [1], the reason for this inadequacy is that the DAA reduces to the PWA for  $n = 0$  response, which severely attenuates the rather low-frequency axisymmetric motion characterizing the inelastic response.

To gain insight into possible improvement of the situation just described, response calculations for  $P_I = 4 P_C$ ,  $T_I = 4$  were performed using the cylindrical wave approximation (CWA) [13]. Utilization of this approximation in the present

problem merely involves taking  $\phi_{RN} = 0$  in (1). Displacement response histories for  $n = 0$  and  $n = 1$  extensional motion produced by RPF-DYNA, DAA-DYNA and CWA-DYNA are shown in Figure 8. It is seen that the RPF-DYNA histories are bounded by their DAA-DYNA and CWA-DYNA counterparts; unfortunately, the bounds are unacceptably large. Similar histories for  $n = 1$  and  $n = 2$  flexural motion are shown in Figure 9. Here, the RPF-DYNA histories are bounded by their DAA-DYNA and CWA-DYNA counterparts over most of the time span shown; these bounds too are unacceptably large.

### Section 3 CONCLUSION

The extensive calculations performed in this study have provided a rather comprehensive picture of the damage behavior of a submerged, infinite cylindrical shell excited by transverse acoustic waves of rectangular pressure profile. This behavior is summarized in the iso-damage curves of Figure 5.

The calculations have also confirmed the failure of the doubly asymptotic approximation as a satisfactory treatment of the fluid-structure interaction for the inelastically excited, infinite cylindrical shell. Such failure was first indicated by a single response calculation reported in [1]. A similar calculation based on the cylindrical wave approximation has produced, in this study, slightly better, but still unsatisfactory, results.

The reason for the failure of the doubly-asymptotic approximation is simply that, for the axisymmetric response of the infinite cylindrical shell, it reduces to the plane wave approximation, which is only singly asymptotic. Such reduction does not occur, however, for finite three-dimensional bodies; in fact, the DAA is exact for the  $n = 0$  response of a spherical body.

On the assumption (which has yet to be verified) that the DAA is satisfactory for determination of the inelastic response of a submerged spherical shell to transient acoustic waves, the following question arises: How large may the aspect (length/diameter) ratio become before the DAA fails as a satisfactory treatment of the fluid-structure interaction for inelastic shell-response problems? Seeking the answer to this question is a fitting subject of future work.

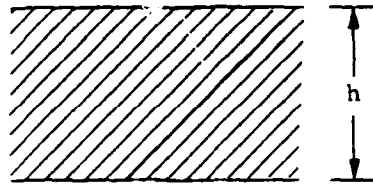
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Table 1. SINGLE-LAYER COMPROMISE AND SANDWICH SHELLS \*

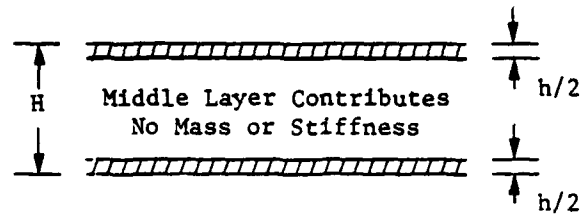
Single-Layer Shell



$$\frac{h}{a} = 0.1$$

$$\frac{\rho_o}{\rho} = 0.772, \frac{c_o}{c} = 3.53, \frac{\sigma_y}{\rho c^2} = 0.02188$$

Sandwich Shell



$$\frac{h}{a} = 0.01, \frac{H}{a} = 0.06266$$

$$\frac{\rho_o}{\rho} = 7.72, \frac{c_o}{c} = 3.53, \frac{\sigma_y}{\rho c^2} = 0.2188$$

Inertial and Elastic Properties

$$"\rho_t" = \frac{\rho_o h}{\rho a} = 0.0772, "E_t" = \frac{\rho_o c_o^2 h}{\rho c^2 a} = 0.9620 \quad "\rho_t" = \frac{\rho_o h}{\rho a} = 0.0772, "E_t" = \frac{\rho_o c_o^2 h}{\rho c^2 a} = 0.9620$$

$$"EI" = \frac{\rho_o c_o^2}{\rho c^2} \cdot \frac{1}{12} \left(\frac{h}{a}\right)^3 = 8.017 \times 10^{-4}$$

$$"EI" = \frac{\rho_o c_o^2}{\rho c^2} \cdot \frac{100}{12} \left(\frac{h}{a}\right)^3 = 8.017 \times 10^{-4}$$

Static-Elastic-Stability and Extensional Elastic-Limit Characteristics

$$P_c = \frac{1}{2} \left(\frac{\rho_o}{\rho}\right) \left(\frac{c_o}{c}\right)^2 \left(\frac{h}{a}\right)^3 = 2.405 \times 10^{-3}$$

$$P_c = 25 \left(\frac{\rho_o}{\rho}\right) \left(\frac{c_o}{c}\right)^2 \left(\frac{h}{a}\right)^3 = 2.405 \times 10^{-3}$$

$$N_y = \left(\frac{h}{a}\right) \left(\frac{\sigma_y}{\rho c^2}\right) = 2.462 \times 10^{-3} **$$

$$N_y = \left(\frac{h}{a}\right) \left(\frac{\sigma_y}{\rho c^2}\right) = 2.462 \times 10^{-3} **$$

Inelastic Flexural Characteristics

$$M_y = 4.103 \times 10^{-5}$$

Yield Moment

$$M_y = 6.549 \times 10^{-5}$$

$$K_y = 0.05118$$

Yield Curvature

$$K_y = 0.08170$$

$$M_u = 6.155 \times 10^{-5}$$

Ultimate Moment

$$M_u = 7.099 \times 10^{-5}$$

\* See Figure 1 for parameter definitions

\*\* von Mises yield condition with  $\nu = 0.3$

Table 2. RPF-DYNA RUNS: SET STRAIN SUMMARY

Format

Maximum Extensional Set Strain Magnitude,  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$   $\hat{P}_I = P_I/P_C$   
 Circumferential Location Where Maximum Occurs  
 Percentage Contribution of  $n=0$  Set Strain to  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$   
 Percentage Contribution of  $n=1$  Extensional Set Strain to  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$   
 Percentage Contribution of  $n=2$  Extensional Set Strain to  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$   
 Approximate Ratio of  $|e_{\text{flex}}^{\text{set}}|_{\text{max}}$  to  $|e_{\text{ext}}^{\text{set}}|_{\text{max}}$

$T_I = \frac{1}{2}, \hat{P}_I = 12$	$T_I = \frac{1}{2}, \hat{P}_I = 20$	$P_I = \frac{1}{2}, \hat{P}_I = 28$
1.823%	5.659%	11.39%
120°	0°	0°
78%	66%	61%
11%	9%	19%
12%	16%	15%
0.06	0.02	0.00
$T_I = 1, \hat{P}_I = 3.6$	$T_I = 1, \hat{P}_I = 12$	$T_I = 1, \hat{P}_I = 18$
1.089%	6.159%	12.40%
0°	0°	70°
41%	78%	87%
16%	10%	5%
20%	9%	7%
0.15	0.01	0.27
$T_I = 2, \hat{P}_I = 3$	$T_I = 2, \hat{P}_I = 5$	$T_I = 2, \hat{P}_I = 9$
1.861%	4.801%	12.09%
0°	0°	0°
55%	63%	80%
24%	14%	18%
12%	13%	0%
0.06	0.03	0.06
$T_I = 4, \hat{P}_I = 1.8$	$T_I = 4, \hat{P}_I = 3.6$	$T_I = 4, \hat{P}_I = 4.2$
1.388%	8.305%	11.09%
60°	0°	0°
69%	64%	66%
7%	23%	23%
8%	10%	9%
0.07	0.02	0.01
$T_I = 6, \hat{P}_I = 1.7$	$T_I = 6, \hat{P}_I = 2.2$	$T_I = 6, \hat{P}_I = 3$
1.890%	4.730%	11.09%
60°	50°	0°
89%	73%	66%
0%	20%	27%
5%	2%	7%
0.04	0.08	0.00
$T_I = 10, \hat{P}_I = 1.2$	$T_I = 10, \hat{P}_I = 1.8$	$T_I = 10, \hat{P}_I = 2.2$
1.182%	5.972%	12.41%
180°	70°	40°
83%	89%	78%
11%	3%	20%
5%	8%	2%
0.10	0.42	0.41



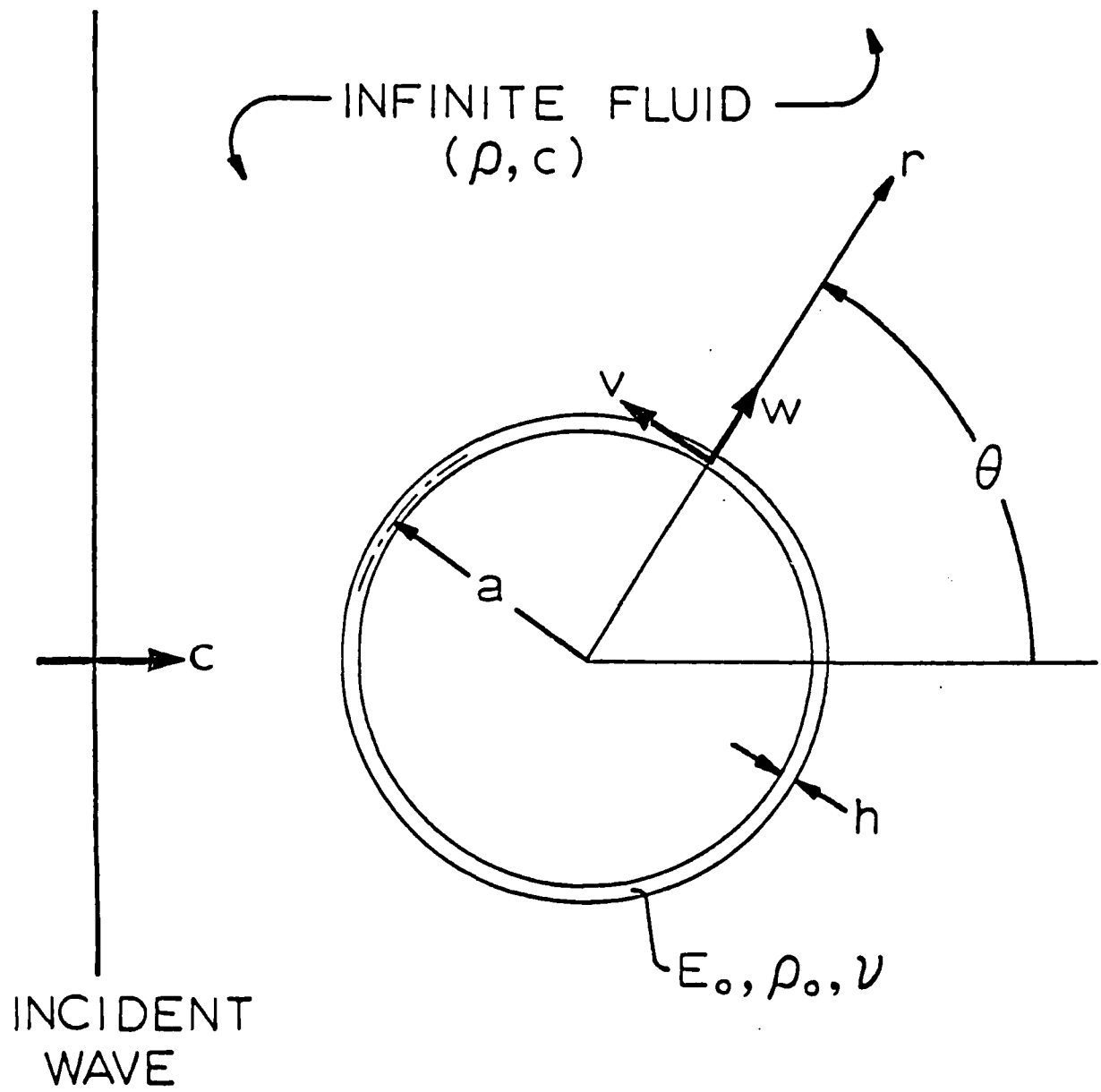


Figure 1. Geometry of Problem

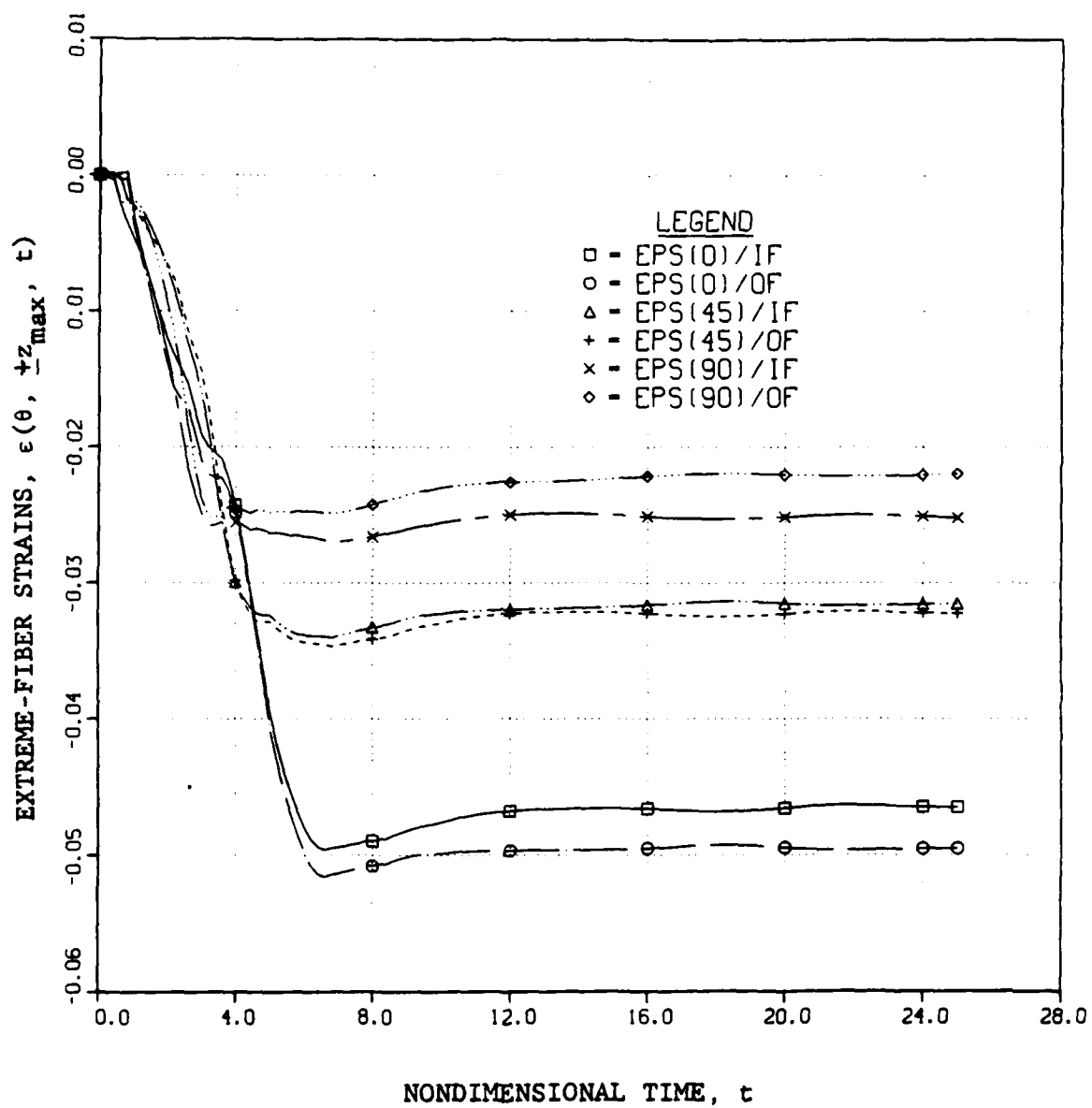


Figure 2 Representative RPF-DYNA Strain Response of Compromise Shell (IF denotes inner fiber; OF denotes outer fiber;  $P_I = 4P_c \approx 4P_o$ ,  $T_I = 4$ )

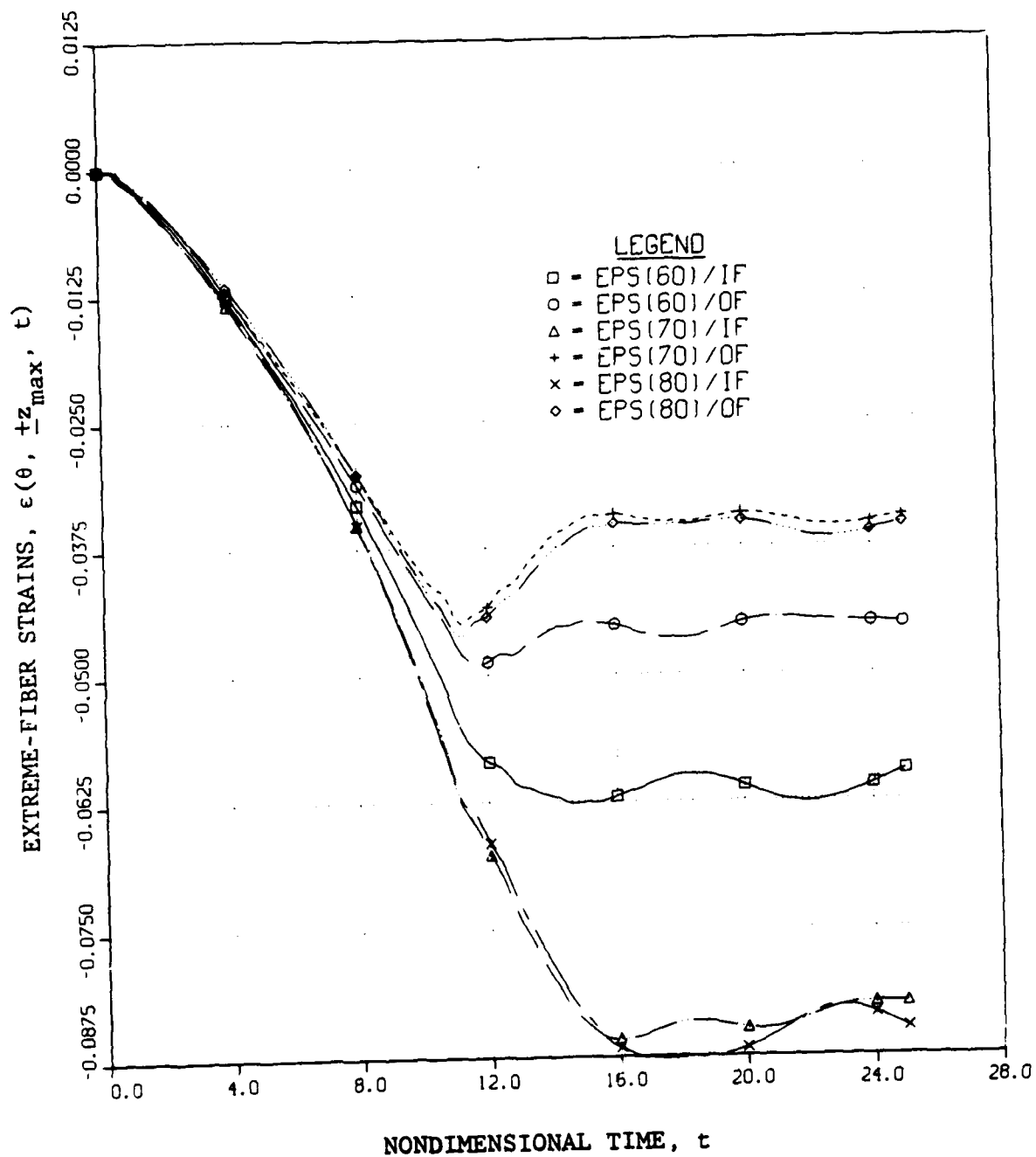


Figure 3 Unrepresentative RPF-DYNA Strain Response of Compromise Shell (IF denotes inner fiber; OF denotes outer fiber;  $P_I = 4P_c \approx 4P_o$ ,  $T_I = 4$ )

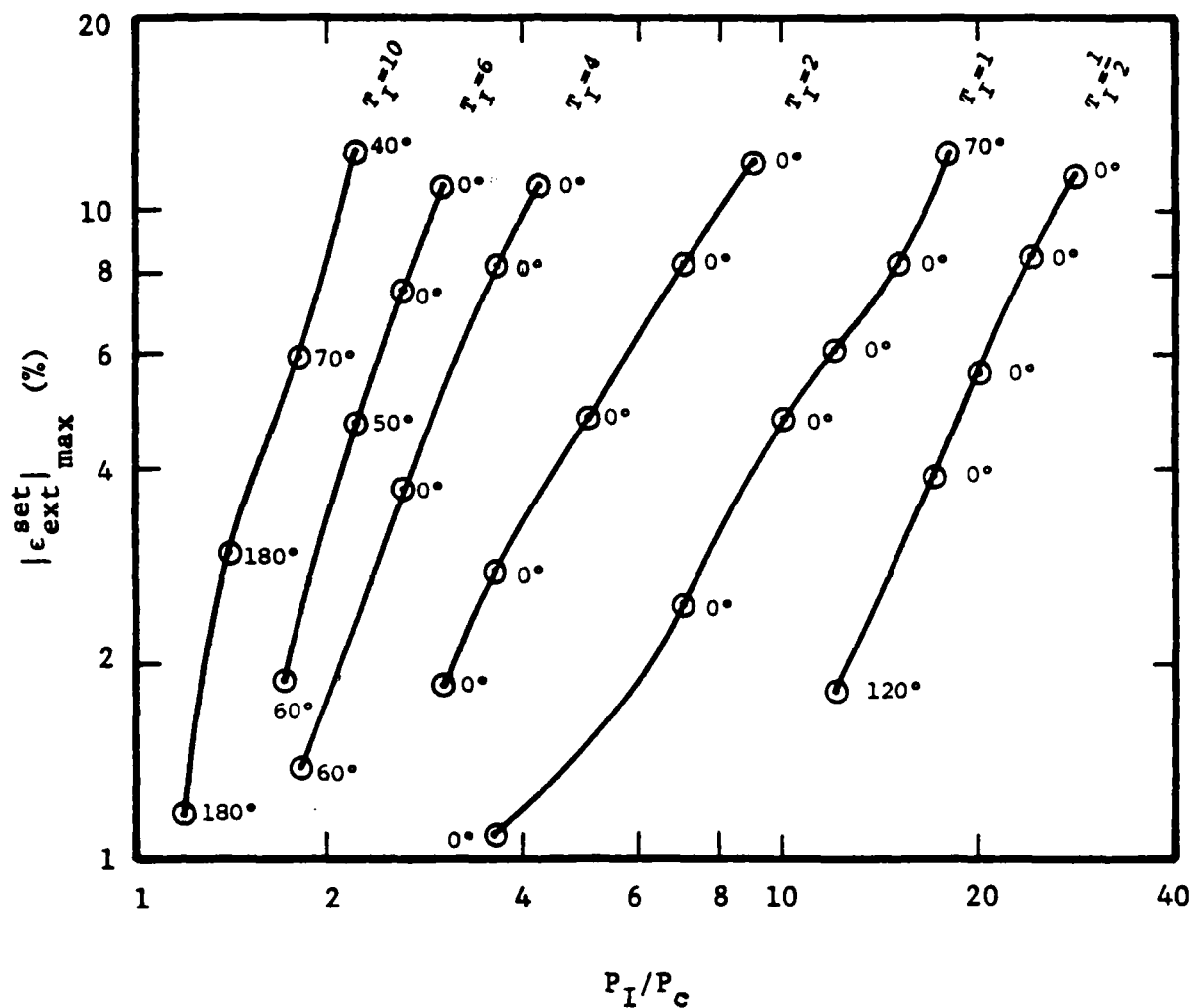


Figure 4 Maximum Extensional Set-Strain Magnitudes as Calculated by RPF-DYNA (angles indicate the locations at which the maxima are reached)

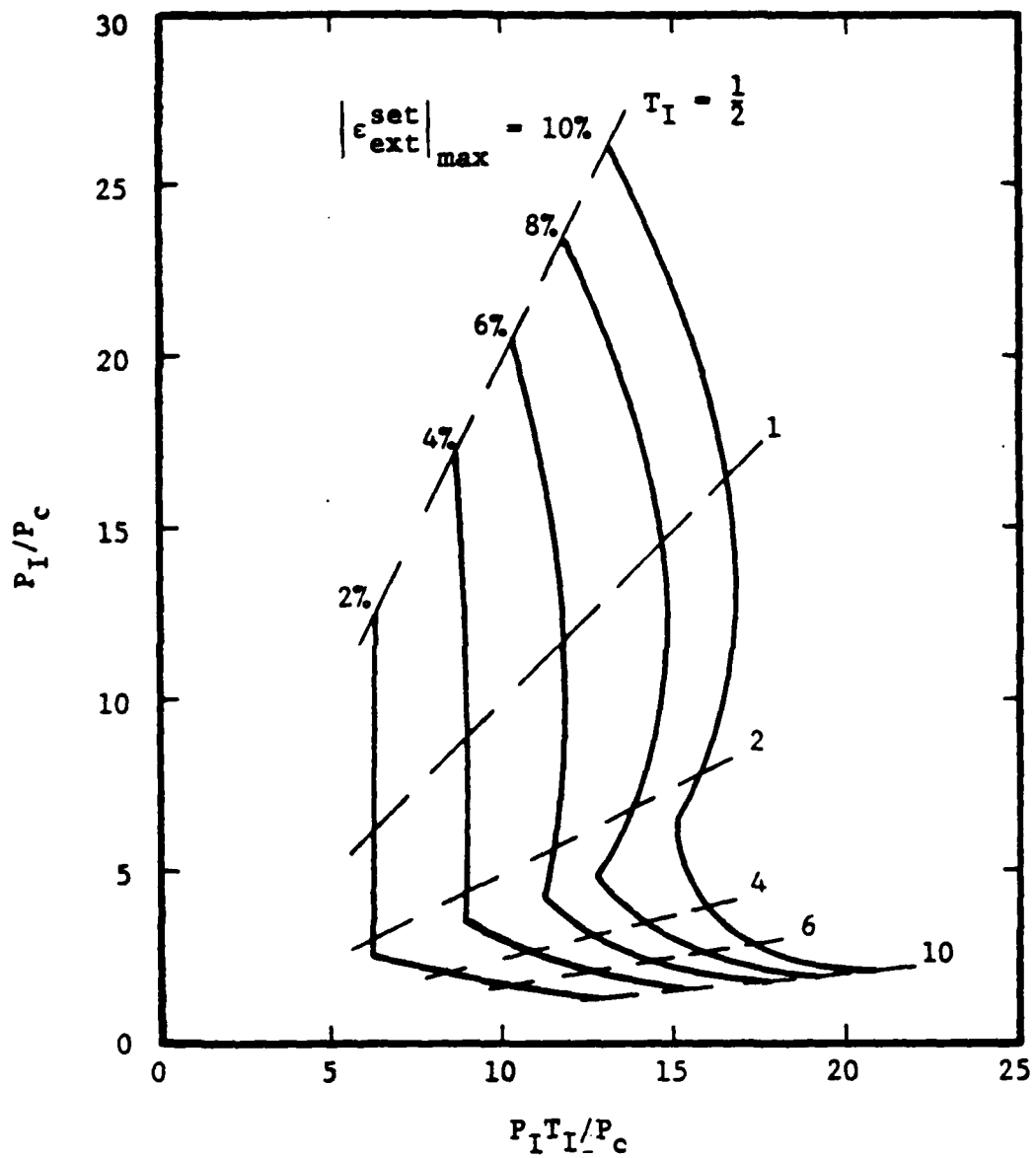


Figure 5 RPF Iso-Damage Curves from the Data of Figure 4

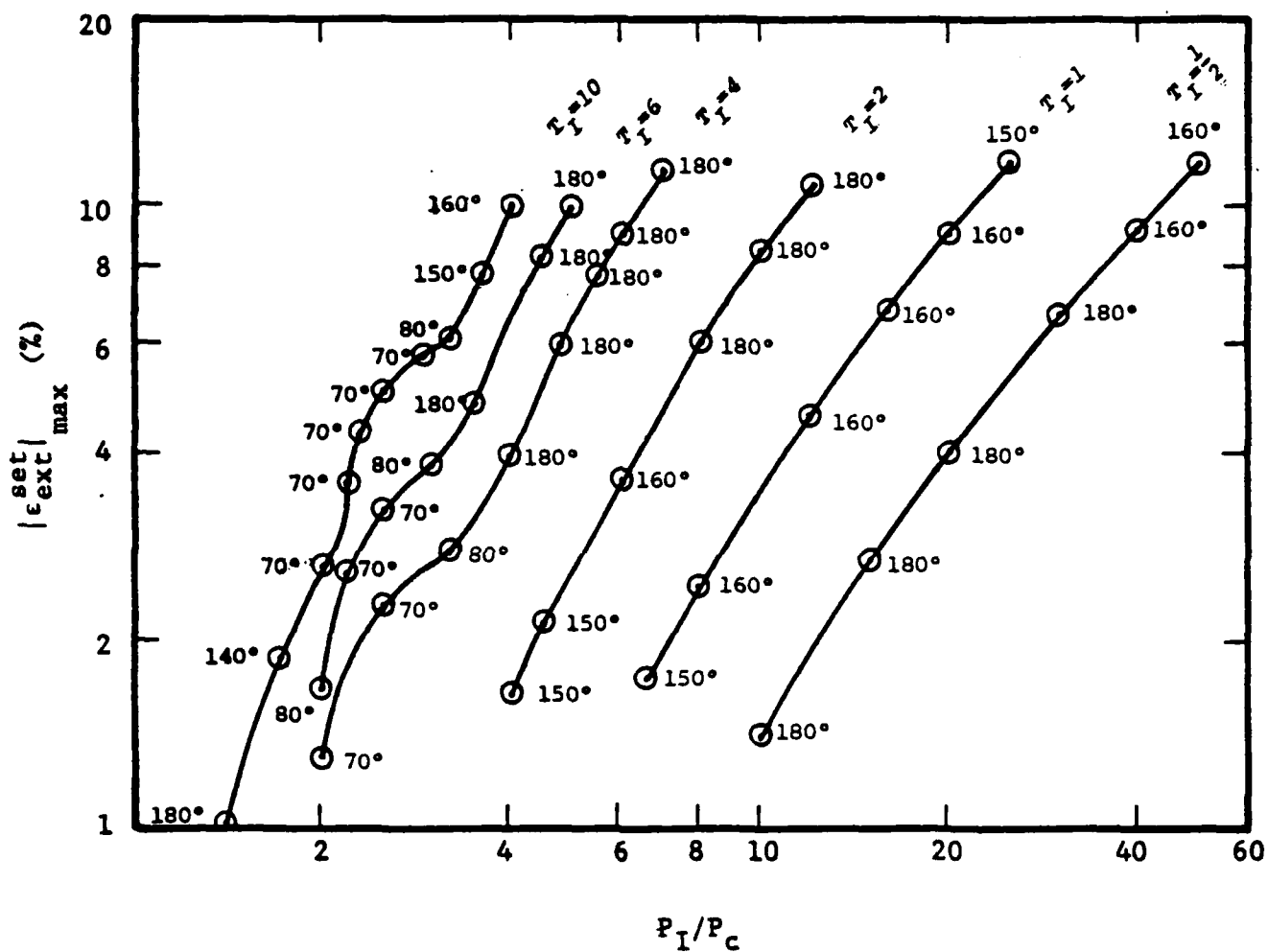


Figure 6 Maximum Extensional Set-Strain Magnitudes as Calculated by DAA-DYNA (angles indicate the locations at which the maxima are reached)

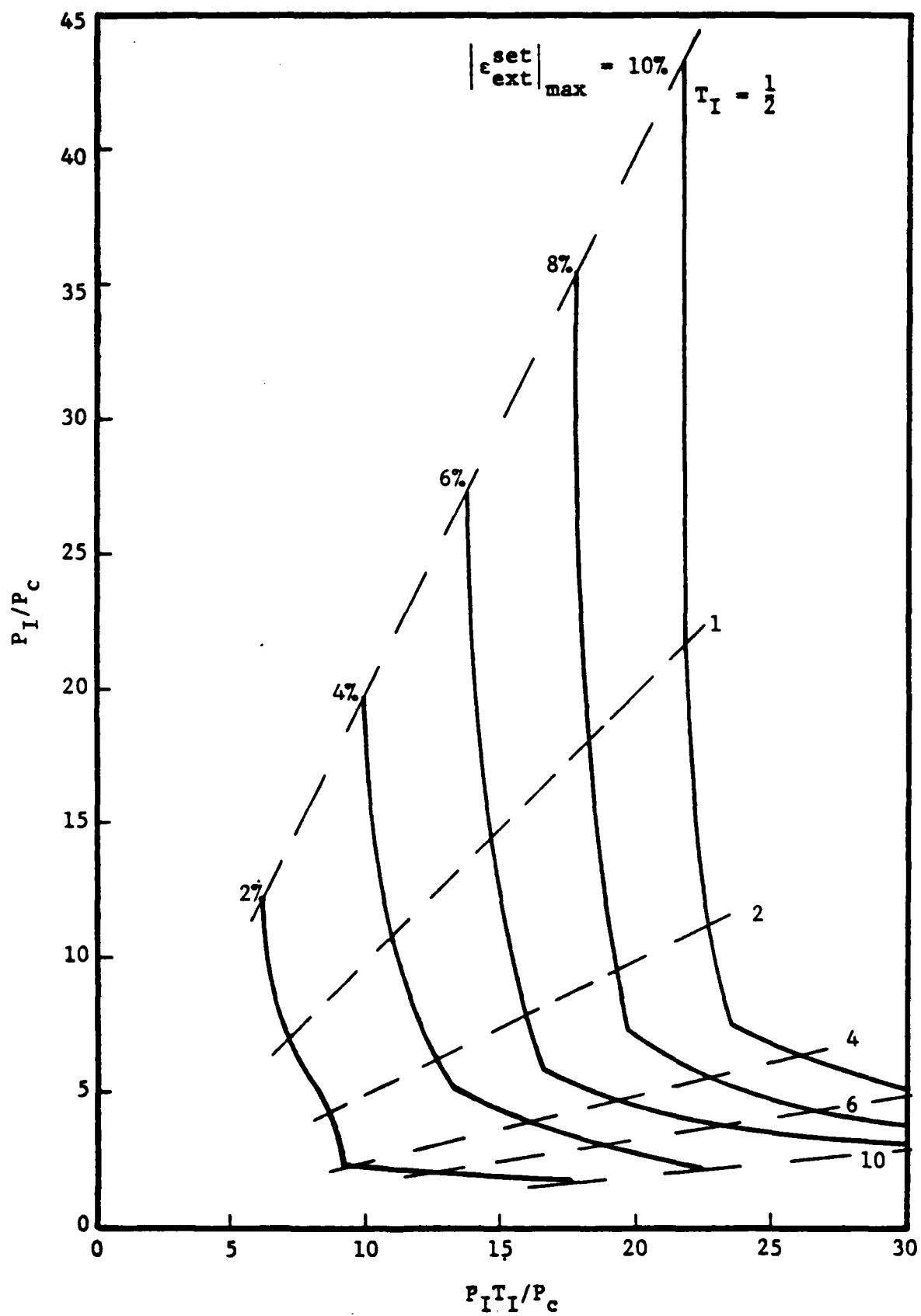


Figure 7 DAA Iso-Damage Curves from the Data of Figure 6

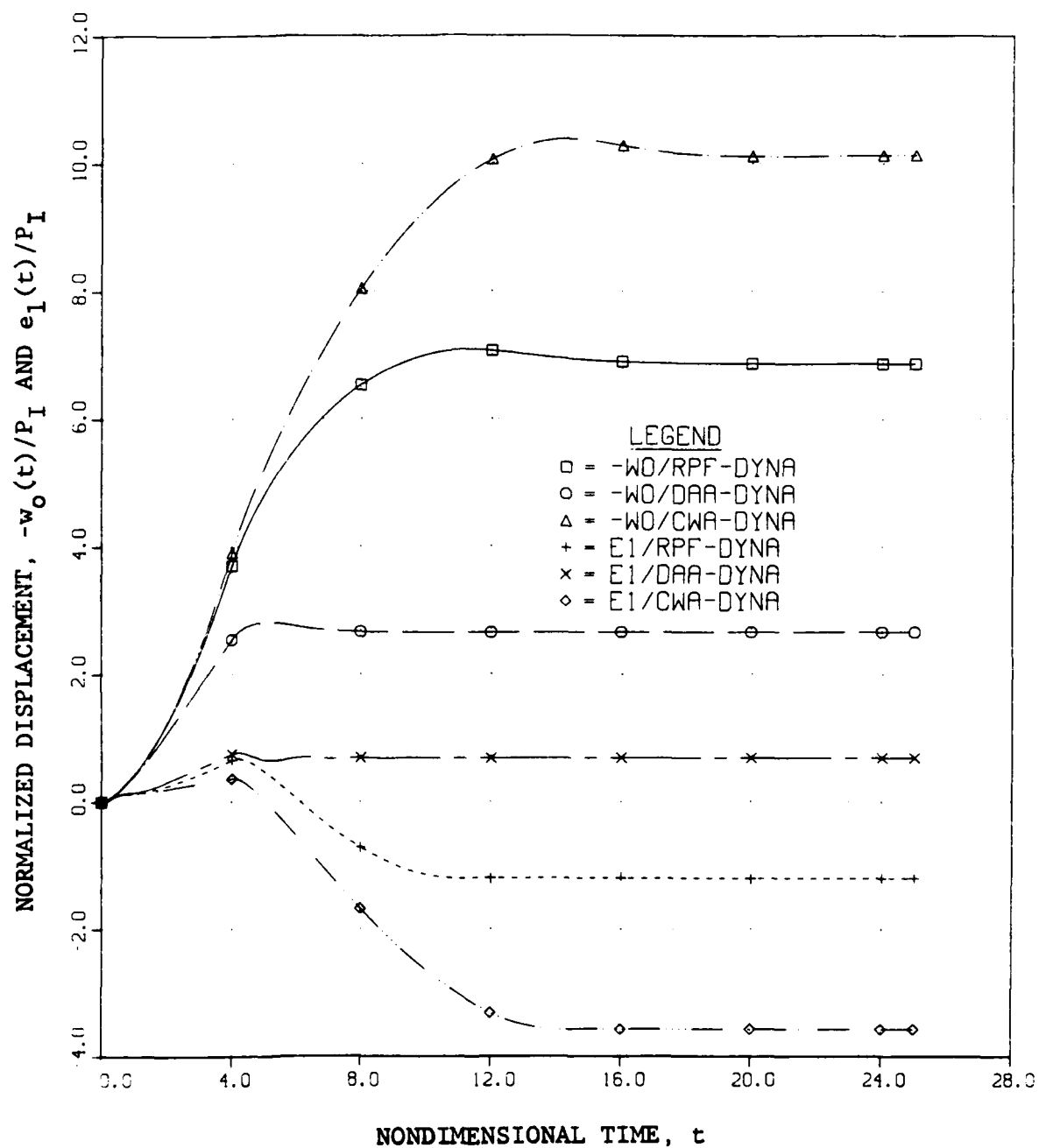


Figure 8  $n=0$  and  $n=1$  Extensional Displacement Response of Compromise Shell as Computed with RPF-DYNA, DAA-DYNA and CWA-DYNA ( $P_I = 4P_c \approx 4P_o$ ,  $T_I = 4$ )



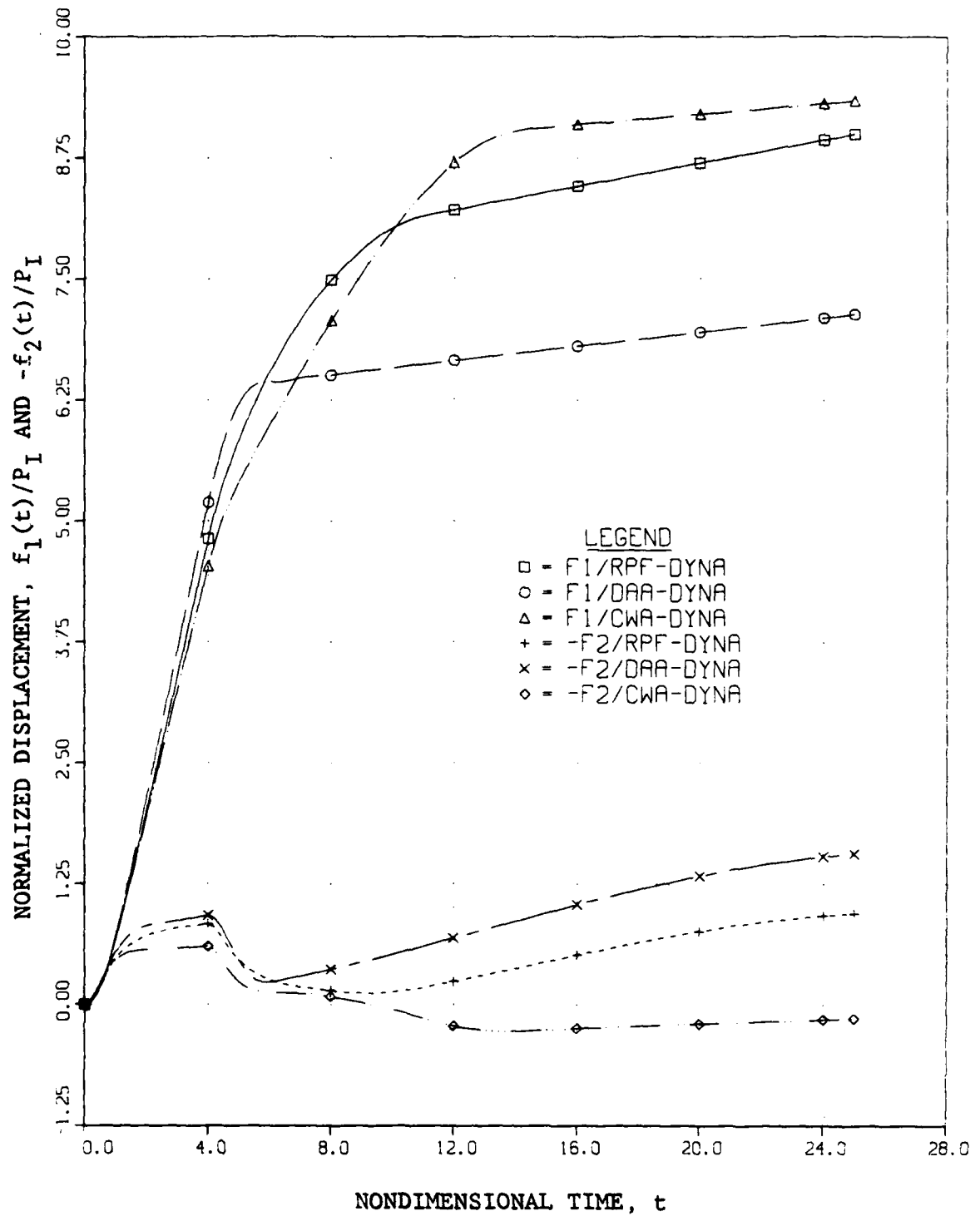


Figure 9  $n=1$  and  $n=2$  Flexural Displacement Response of Compromise Shell as Computed with RPF-DYNA, DAA-DYNA and CWA-DYNA ( $P_I = 4P_c \approx 4P_o$ ,  $T_I = 4$ )

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20. ABSTRACT

↓ appreciably from their exact counterparts. ↑

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